



Math Virtual Learning

Algebra 2/Honors Algebra 2

May 6, 2020



Lesson: May 6, 2020

Objective/Learning Target:

Students will be able to solve rational equations.

Let's Get Started:

On a sheet of paper, answer the question...

What's the difference?

$$\frac{x^2 + 7x + 10}{x^2 - 4} + \frac{3}{x}$$

and

$$\frac{x^2 + 7x + 10}{x^2 - 4} = \frac{3}{x}$$

(Hint, look at the symbols.)

Watch the Video:

Take notes as you watch the video below.

Solving Rational Equations

$$\frac{4}{x} + \frac{8}{x+2} = 4 \qquad \frac{4}{x-3} = \frac{9}{x+2}$$

$$\frac{x}{x+5} - \frac{5}{x-5} = \frac{14}{x+5} \qquad \frac{9}{x} = \frac{x}{4}$$

$$x + \frac{8}{x} = 6 \qquad \frac{x+3}{x-3} = \frac{12}{3}$$

Steps for solving a rational equation:

(write this down)

- factor the denominators
- find the LCD
- identify the domain
- multiply each term by ALL of the LCD
- cancel and solve
- check for extraneous solutions

Example #1

Given

$$\frac{5}{x} + \frac{7}{4} = -\frac{9}{x}$$

Problem:

LCD: $4x$

Domain: $x \neq 0$

$$\cancel{4x} \cdot \frac{5}{\cancel{x}} + \frac{7}{4} = -\frac{9}{\cancel{x}}$$

$$\begin{array}{r} 20 + 7x = -36 \\ -20 \quad \quad -20 \\ \hline 7x = -56 \\ \frac{7x}{7} = \frac{-56}{7} \\ x = -8 \end{array}$$

Example #2

Given

Problem:

$$1 - \frac{8}{x-5} = \frac{3}{x}$$

LCD: $x(x-5)$

Dom: $x \neq 5$
 $x \neq 0$

$$\frac{1}{1} - \frac{8}{\cancel{(x-5)}} = \frac{3}{\cancel{x}}$$

(Note: In the original image, the denominators are crossed out and replaced with x(x-5) for the LCD.)

$$1x(x-5) - 8x = 3(x-5)$$

$$x^2 - 5x - 8x = 3x - 15$$

$$x^2 - 13x = 3x - 15$$

$$-3x + 15$$

$$x^2 - 16x + 15 = 0$$

$$(x-15)(x-1) = 0$$

$$\boxed{x=15} \quad \boxed{x=1}$$

$$1) \frac{4}{x} + x = 5$$

$$2) \frac{2}{3x} + \frac{1}{6} = \frac{4}{3x}$$

$$3) \frac{1}{2x} + \frac{3}{x+7} = -\frac{1}{x}$$

$$4) \frac{1}{x-2} + 2 = \frac{3x}{x+2}$$

$$5) \frac{x+1}{x+6} + \frac{1}{x} = \frac{2x+1}{x+6}$$

$$6) \frac{2}{x-3} + \frac{1}{x} = \frac{x-1}{x-3}$$

$$7) \frac{18}{x^2-3x} - \frac{6}{x-3} = \frac{5}{x}$$

$$8) \frac{x+3}{x-3} + \frac{x}{x-5} = \frac{x+5}{x-5}$$

Solving Rational Equations Practice:

On the same sheet of paper, solve the following practice problems. Remember to check if your solutions work or are extraneous.

Solving Rational Equations Answer Key:

Once you have completed the problems, check your answers here.

1) $x = 1$ and $x = 4$

2) $x = 4$

3) $x = -\frac{7}{3}$

4) $x = 1$ and $x = 6$

5) $x = -2$ and $x = 3$

6) $x = 1$

7) *no solution*

8) $x = 0$ and $x = 7$

Additional Practice:

Click on the links below to get additional practice and to check your understanding!

Solving Rational Equations:

[Notes](#), [Practice](#), & [Answer Key](#)

Solving Rational Equations [Website - Practice Problems](#)